

Useful identities

1. $\int x^n dx = \frac{1}{n+1}x^{n+1} + C \quad (n \neq -1)$
2. $\int \frac{1}{x} dx = \ln|x| + C$
3. $\int \sin x dx = -\cos x + C$
4. $\int \cos x dx = \sin x + C$
5. $\int \sec^2 x dx = \tan x + C$
6. $\int \csc^2 x dx = -\cot x + C$
7. $\int \csc x \cot x dx = -\csc x + C$
8. $\int \sec x \tan x dx = \sec x + C$
9. $\int e^x dx = e^x + C$
10. $\int \tan x dx = -\ln|\cos x| + C$
11. $\int \cot x dx = \ln|\sin x| + C$
12. $\int \sec x dx = \ln|\sec x + \tan x| + C$
13. $\int \csc x dx = -\ln|\csc x + \cot x| + C$
14. $\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1}\left(\frac{x}{a}\right) + C$
15. $\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1}\left(\frac{x}{a}\right) + C$
16. $\int \frac{1}{x\sqrt{x^2 - a^2}} dx = \frac{1}{a} \sec^{-1}\left(\frac{|x|}{a}\right) + C$
17. $\int \sec^3 x dx = \frac{1}{2} (\sec x \tan x + \ln|\sec x + \tan x|) + C$
18. $\sin(2x) = 2 \sin x \cos x$
19. $\cos(2x) = \cos^2 x - \sin^2 x = 1 - 2 \sin^2 x = 2 \cos^2 x - 1$
20. $\cos^2 x = \frac{1 + \cos(2x)}{2}$
21. $\sin^2 x = \frac{1 - \cos(2x)}{2}$